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# Adapting GDOI for Balanced Batch LKH

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# Introduction

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## ❑ Goal of the work:

- Studying the behavior of batch rekeying in real scenarios and improving Lam-Gouda's algorithm.

## ❑ Roadmap:

- Generating synthetic user behavior patterns (according to benchmark scenarios) in order to simulate performance behavior of batch rekeying algorithms
- Simulate and detect flaws of proposed batch rekeying algorithm
- Propose a slight variation in the algorithm
- Introduce broadcast encryption in multicast key management for single and batch processing
- Adapt the algorithms to GDOI
- Implementation of LKH and variation algorithms in GDOI

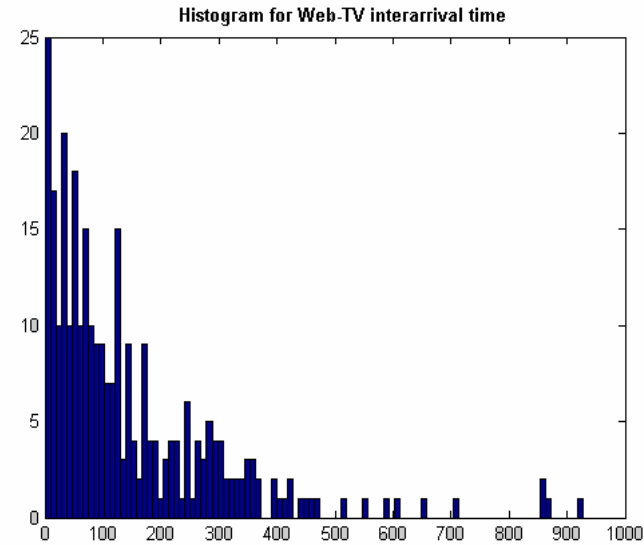
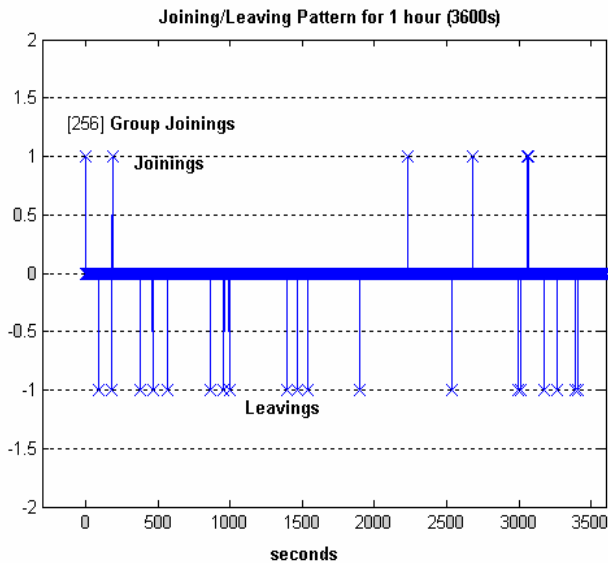
# Benchmark Scenarios

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- R. Canetti, J. Garay, G. Itkis, D. Micciancio, M. Naor, and B. Pinkas, **Multicast security: A taxonomy and some efficient constructions** INFOCOM 99. Eighteenth Annual Joint Conference of the IEEE Computer and Communications Societies. Proceedings. IEEE, vol. 2, pp. 708-716, 1999.
  
- **2 benchmark scenarios pointed out :**
  - single source broadcast
  - virtual conferences
  
- **One more scenario included :**
  - netgames
  
- **All patterns generated in Matlab**

# Benchmark Scenarios

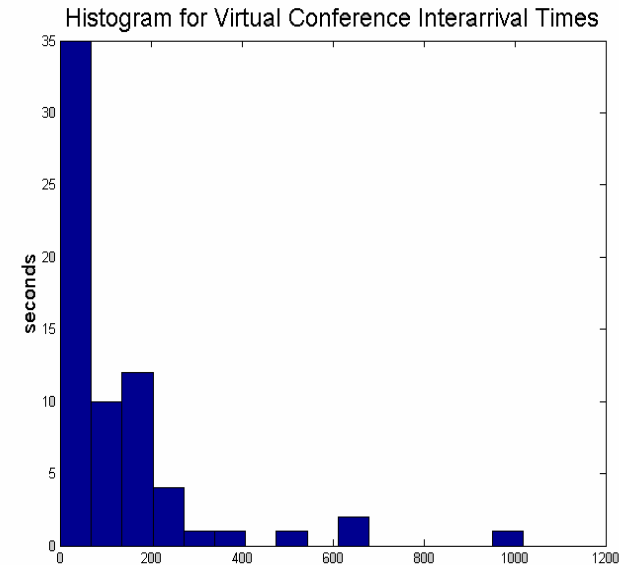
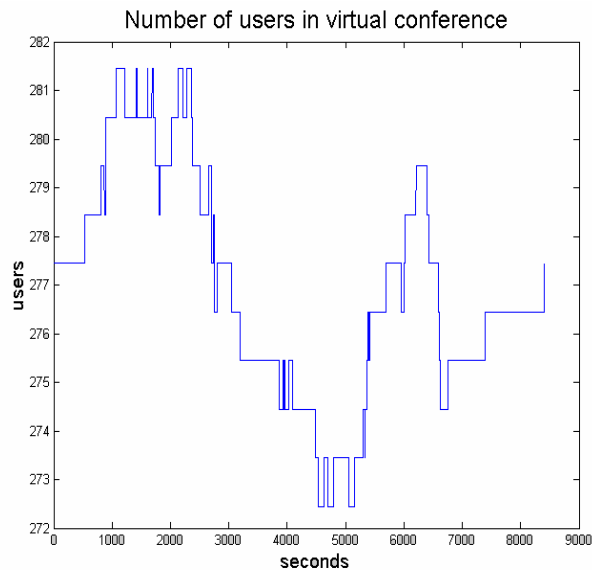
## □ Single source broadcast



- Exponential distribution inter-arrival time
- Based on the classic study of Almeroth and Ammar  
(Multicast Group Behavior in the Internet's Multicast Backbone (Mbone), IEEE Communications, June 1997)
- Mean value of Inter-arrival time can be set by desing

# Benchmark Scenarios

## Virtual conferences

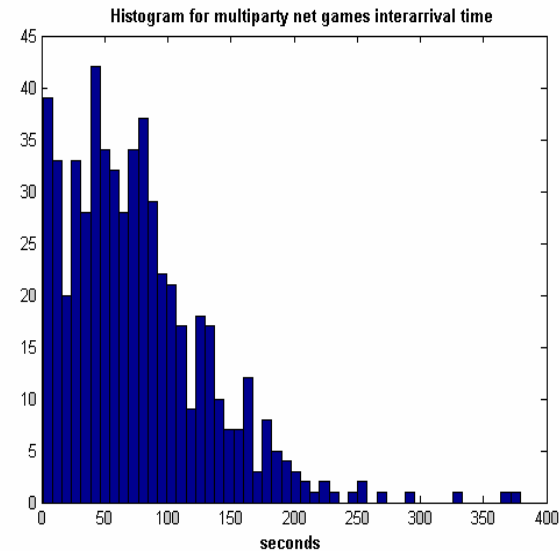
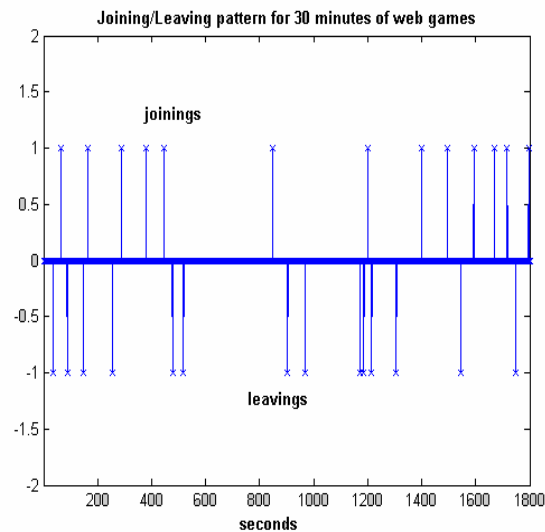


- A random number of users establish a virtual conference
- After a random period of time users begin to join/leave the group following an exponential inter-request time statistics

# Benchmark Scenarios

## □ Networked games

- Henderson, Bhatti (2001). **Modeling user behavior in networked games**. Proceedings of ACM Multimedia 2001, Ottawa, Canada, pp212-220, October 2001



- **Player interarrival times are highly correlated at short lags which implies that the arrival of some users will lead to others arriving**
- **Interarrival times for networked games follow a heavy-tailed distribution**

# Performance of Batch Rekeying with benchmark scenarios

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## Why real patterns should be included?

Li, Yang, Gouda, Lam. **Batch Rekeying for Secure Group Communications**. ACM SIGCOMM 2001, San Diego, August 2001

**Introduce batch processing for Join/Leave requests but simulation results presented does not fit a real request pattern** but a uniformly distributed and only considering the total number of joining and leaving requests but not their position in the tree.

In such cases, it is easy to get an **unbalanced tree** after a few batches.

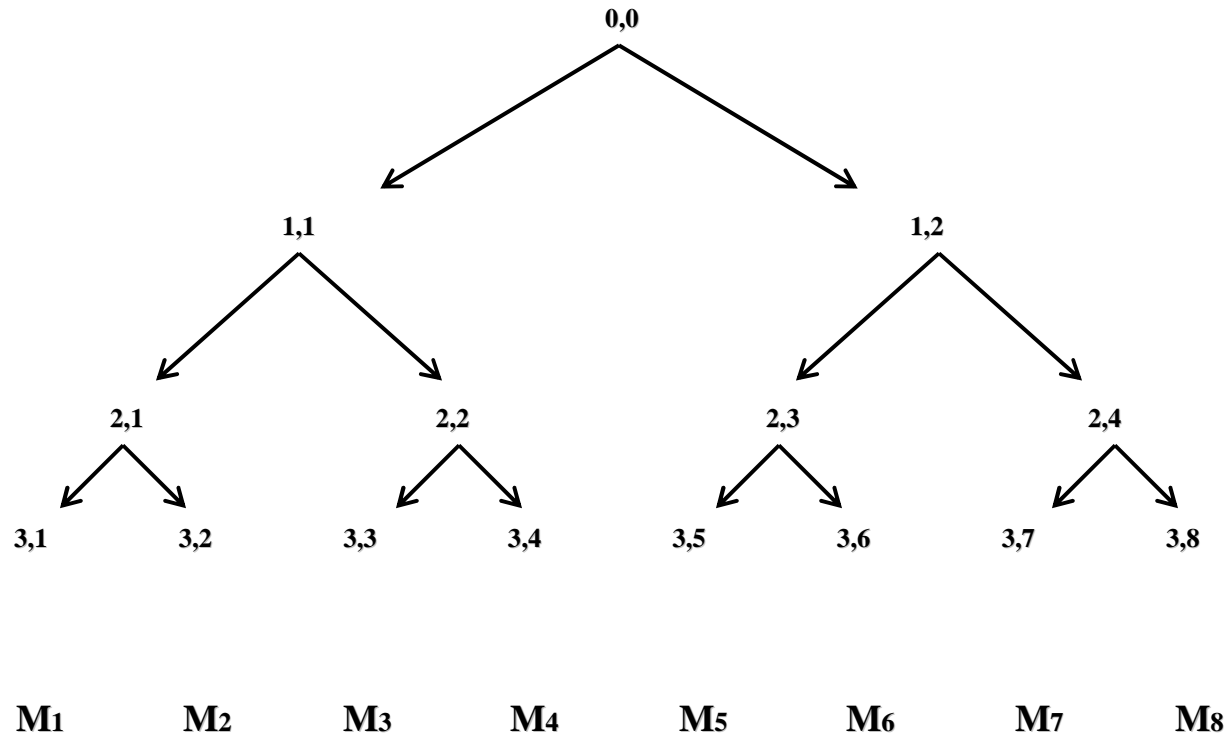
An additional balancing algorithm is suggested after some rekeyings to overcome this flaw

# Lam-Gouda Proposal not balanced

New joinings are located substituting leavings

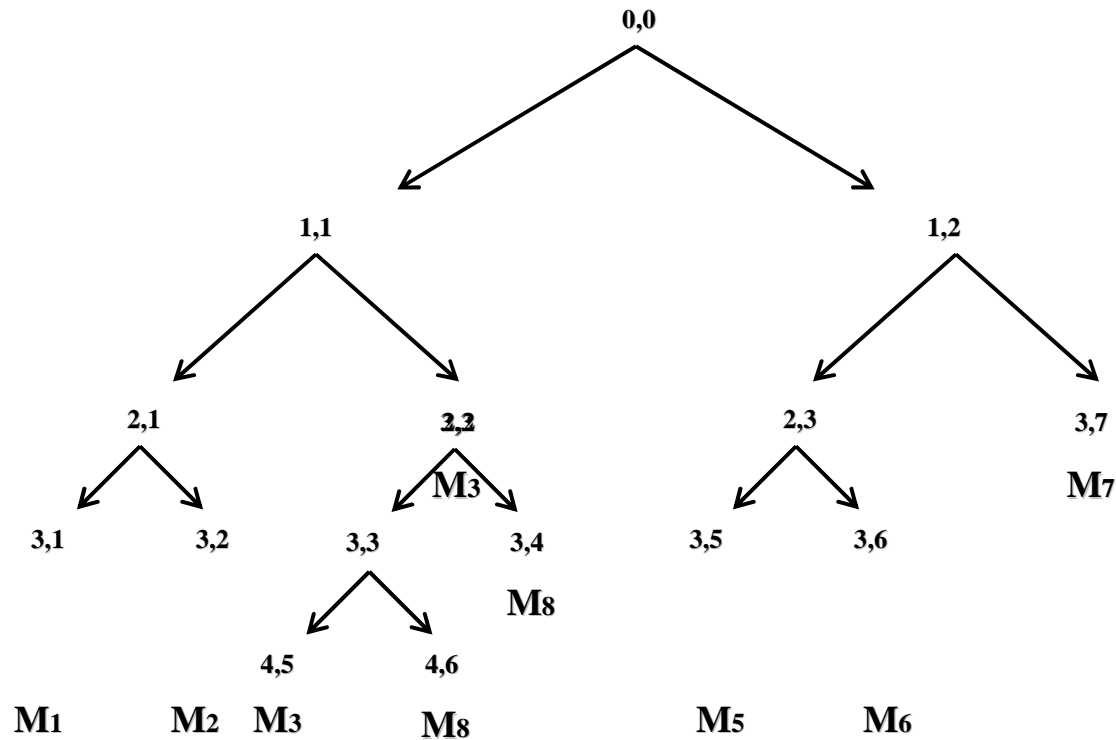
If number of joinings exceeds leavings a subtree is constructed and placed under the shallowest leaf

- Example: Member 4 and Member 8 leave the group



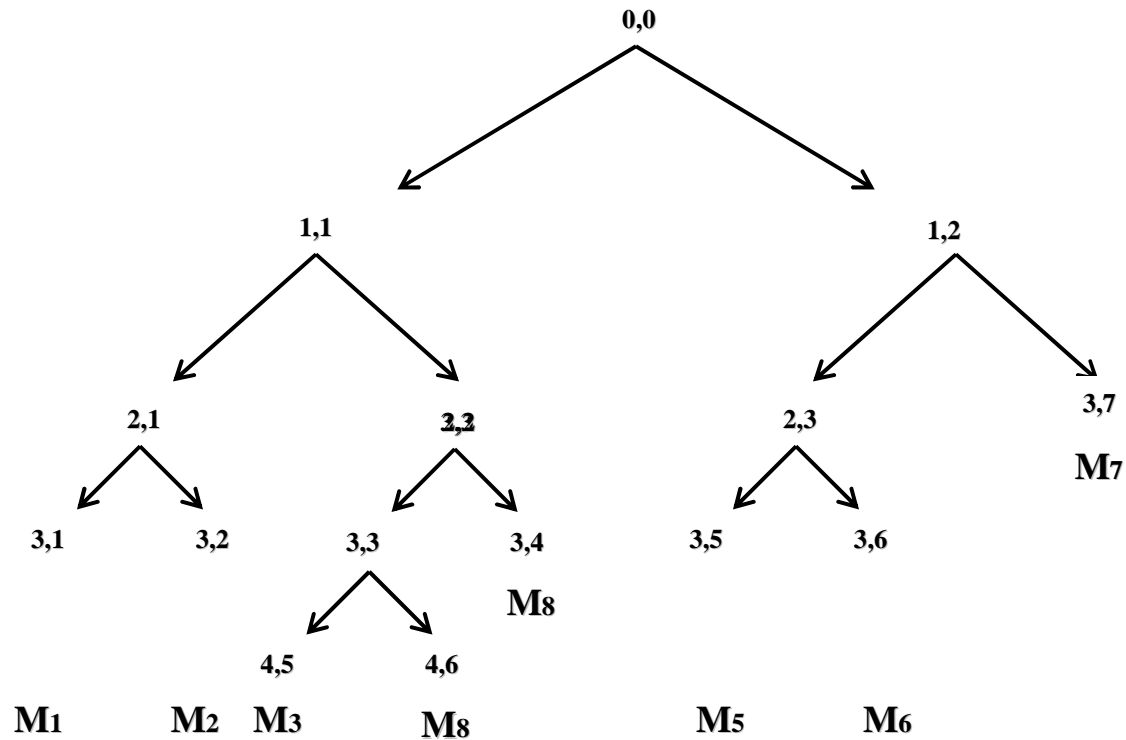
# Lam-Gouda Proposal not balanced

- 2 joinings and no leaving



# Lam-Gouda Proposal not balanced

- M5 and M6 leave the group



# Balanced Batch Rekeying

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Pegueroles, Rico-Novella. **Balanced Batch LKH: New Proposal, Implementation and Performance Evaluation.** IEEE Symposium on Computers and Communications - ISCC'2003, 2003

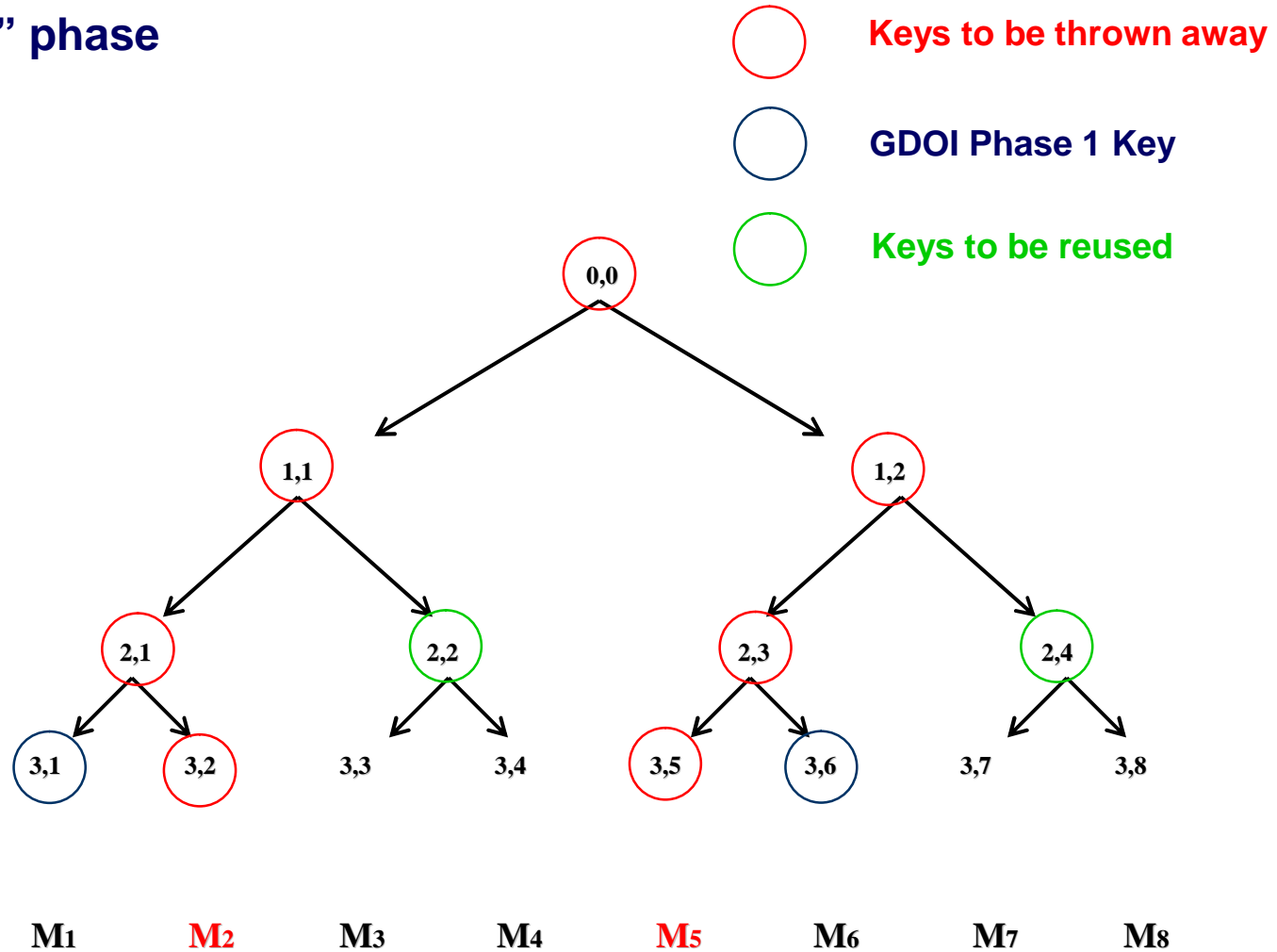
We have **proposed a batch rekeying method leading to completely balanced trees.**

It is **based on the assumption that:**

- **Siblings of departed members are treated as new members** with GDOI phase 1 already done
- **Members can change their position in the tree from one batch to another,** not only in their path to the root but also can jump to another branch.

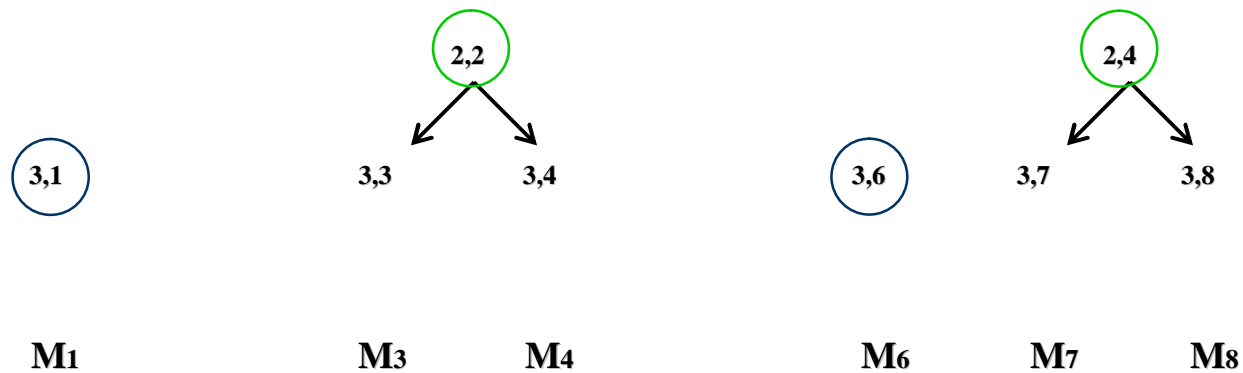
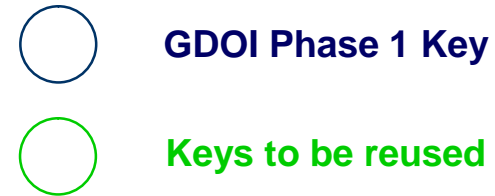
# Balanced Batch Rekeying

“Mark Tree” phase



# Balanced Batch Rekeying

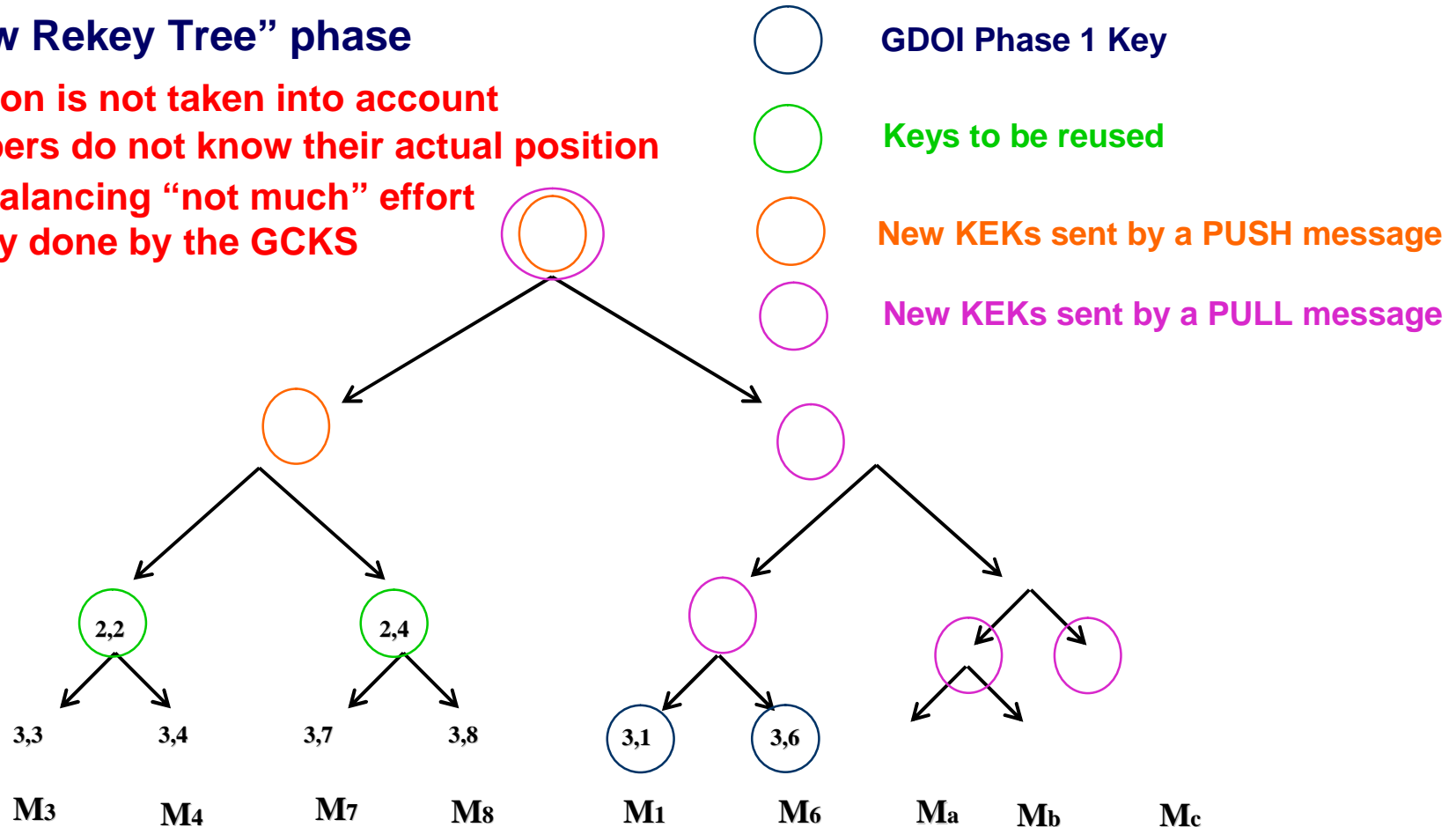
“Prune Tree” phase



# Balanced Batch Rekeying

## “New Rekey Tree” phase

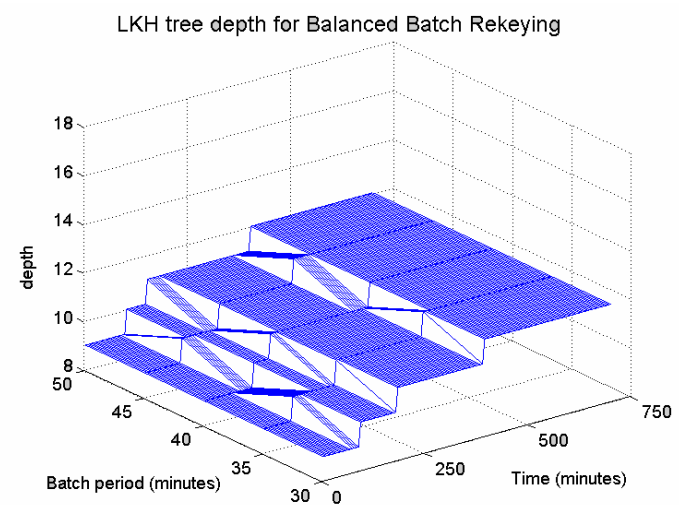
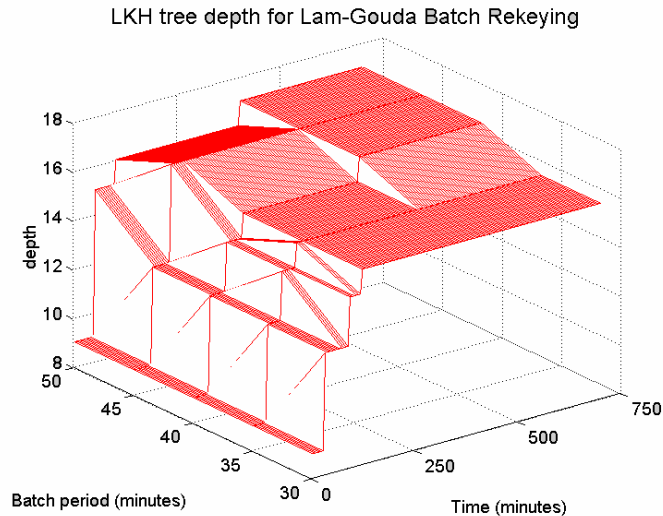
**Position is not taken into account**  
**Members do not know their actual position**  
**The balancing “not much” effort**  
**is only done by the GCKS**



**Only the Key-Handle GDOI's parameter is used**

# Balanced Batch Rekeying

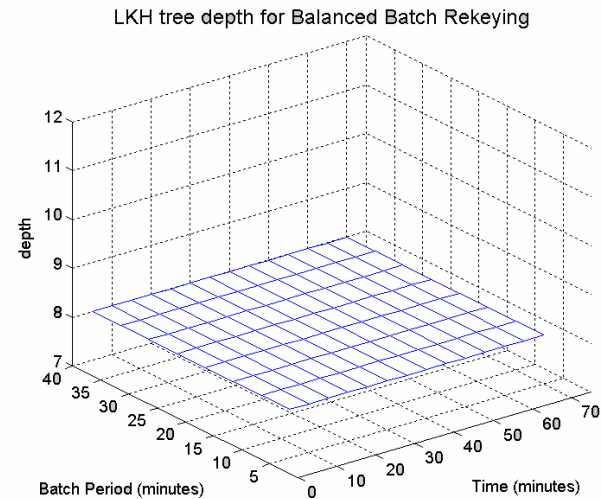
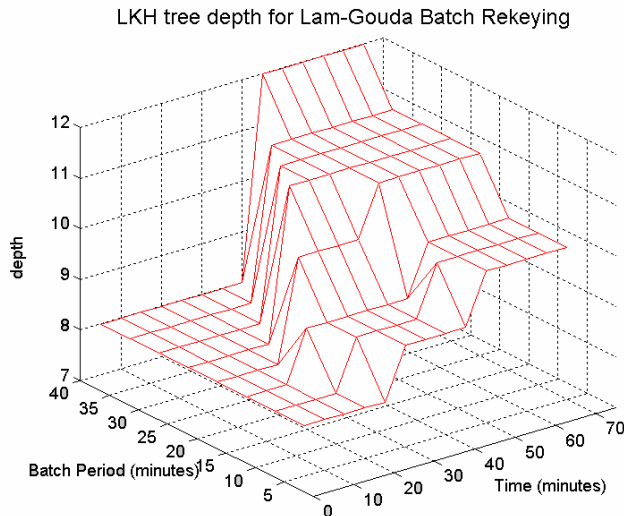
- Tree depth evolution for Lam-Gouda and balanced batch rekeying algorithm in web tv environment



**Effect of the peak arrivals minimized**

# Balanced Batch Rekeying

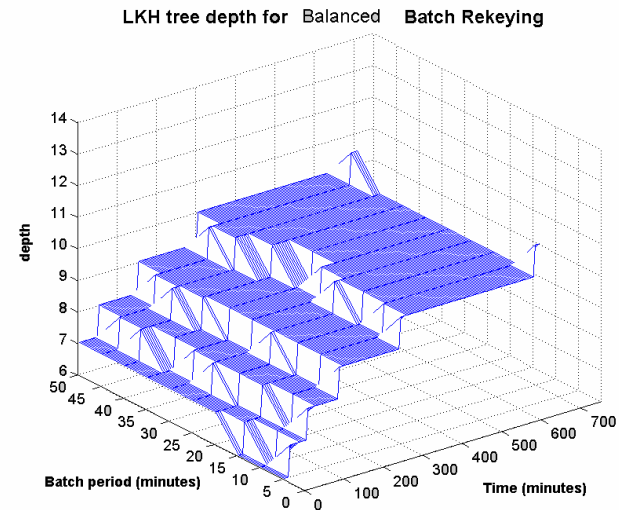
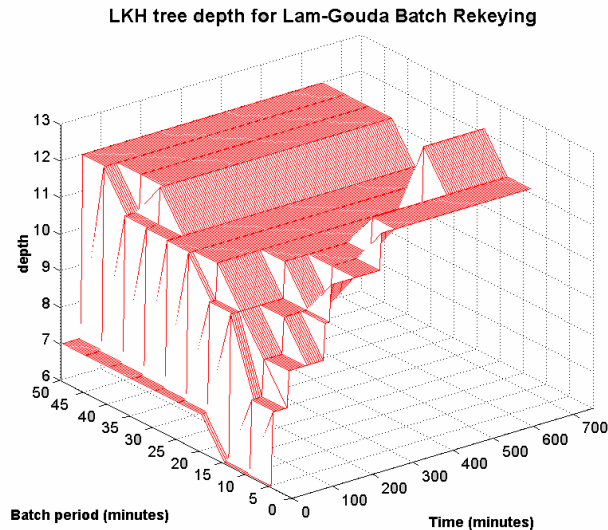
- Tree depth evolution for Lam-Gouda and balanced batch rekeying algorithm in virtual conference environment.



**If number of members is within a range tree depth remains constant**

# Balanced Batch Rekeying

- Tree depth evolution for Lam-Gouda and balanced batch rekeying algorithm in networked games environment



# Balanced Batch Rekeying

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- **We have arrived at the same conclusion as Lam and Gouda:**

Balancing is better...

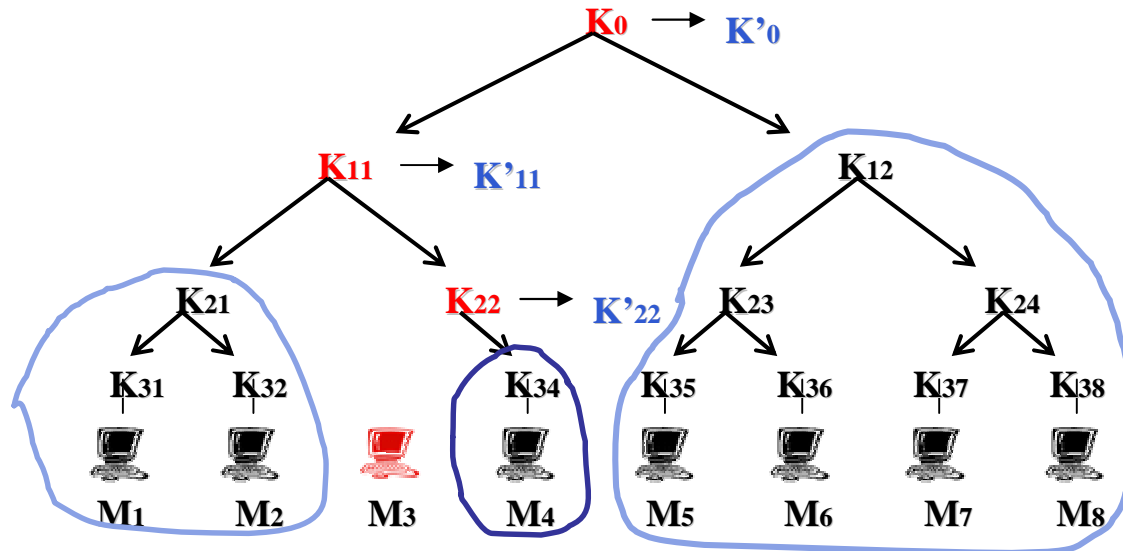
...but we have introduced balancing in the algorithm itself

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## **Introducing Broadcast Encryption: Single message rekeying algorithm**

# Single message rekeying

Assume the following scenario:



We consider the concatenated LKH message

$$K_{34} \{ K_0' \} \quad K_{34} \{ K_{11}' \} K_{34} \{ K_{22}' \} \parallel K_{21} \{ K_0' \} \quad K_{21} \{ K_{11}' \} \parallel K_{12} \{ K_0' \}$$

as **3 messages** cause it is the result of 3 encryption operations. Moreover, parts of this message are not useful for some remaining members.

**We want to generate a single message, the same for all the remaining members.**

We use **number theory and modular reduction.**

# Single message rekeying

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Let every node in the tree be a random number generated as follows:

$$\gg K_{(i,j)} = F_{r1}(2^i+j) \oplus r$$

When the node wants to be updated, the only necessary information is

$$\gg P = r \oplus r'$$

and the updated number will be computed as follows:

$$\gg K'_{(i,j)} = K_{(i,j)} \mathring{\wedge} P = F_{r1}(2^i+j) \mathring{\wedge} r'$$

When updating is needed only  $P$  has to be delivered to the remaining members

**At this moment the GCKS only has to store  $r1$  and  $r'$  and the TEK**

Bin, Jian-Hua. *Optimal Key Storage for Secure Multicast*. Department of Electronic Engineering, Shanghai Jiaotong University

# Single message rekeying

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But, if the multicast message is constructed as follows:

$$P = r_2 \prod_{i \in S} rnd_i + (r \oplus r')$$

We get only one (and the same) message for all the members.

That only have to divide modulo one of his secret numbers in order to obtain the updating parameter.

**Although it can be considered weaker than LKH/OFT/OFC, it provides enough security level for many non critical applications.**

**Security analysis is included in**

Pegueroles, Bin, Rico-Novella, Jian-Hua. **Efficient Multicast Group Rekeying.**

Departamento de Ingenieria Telemática IR 2003.

<http://isg.upc.es/gsec/work.html>

# Single message rekeying

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**But...**

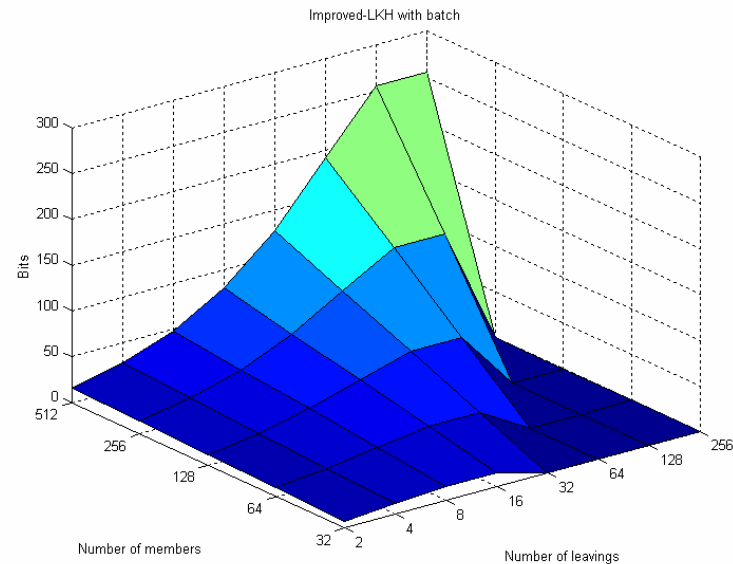
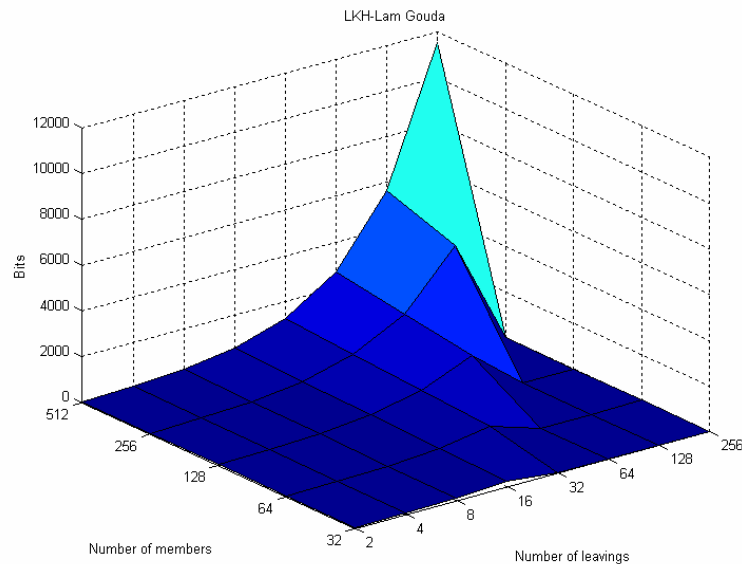
OK, the GCKS only has to store 3 numbers but we have 1 message of length  $KN$  instead of  $N$  messages of length  $K$ ... **where's the improvement?**

**First, the length of the messages needed in simple LKH is greater than each of the numbers of the modulo product.**

**Second, If Batch rekeying is considered...**

# Single message rekeying for batch rekeying

Comparing the total amount of bits used for rekeying in Batch LKH Lam Gouda and batch with single message rekeying...



Pegueroles, Hernandez-Serrano , Rico-Novella, Soriano . **Improved LKH for Batch Rekeying in Multicast Groups**. To appear in the proceedings of the IEEE International Conference on Technology Research and Education (ITRE 2003) New Jersey August 2003.

# Adaptation for GDOI

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- **GDOI perfectly fits with all the mentioned algorithms**
- **Only some considerations of unused parameters in LKH payload message format have to be added**
- **We have started the task of adding LKH to GDOI Brian Weis' implementation**

## Work to do

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- **Discuss the proposed methods:**
  - balanced batch
  - single message rekeying
- **Include them in a standard track LKH/OFT/OFC...**
- **Finishing the implementation of these algorithms in GDOI testbed**

# Contact Information

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